



Province of the
EASTERN CAPE
EDUCATION

**NATIONAL
SENIOR CERTIFICATE/
NASIONALE
SENIOR SERTIFIKAAT**

GRADE/*GRAAD* 10

NOVEMBER 2020




**TECHNICAL MATHEMATICS P1/
TEGNIESE WISKUNDE V1
MARKING GUIDELINE/*NASIENRIGLYN*
(*EXEMPLAR/EKSEMPLAAR*)**

MARKS/*PUNTE*: 100

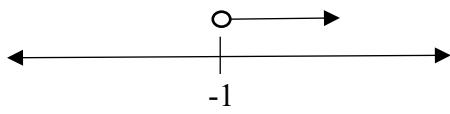
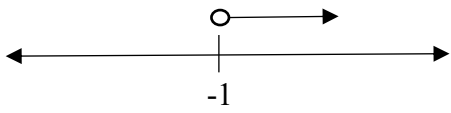
This marking guideline consists of 9 pages./
Hierdie nasienriglyn bestaan uit 9 bladsye.


QUESTION/VRAAG 1																																							
NO.	SOLUTION/OPLOSSING	EXPLANATION/ VERDUIDELIKING																																					
1.1.1	$\sqrt[3]{27}$	✓ Answer / <i>antwoord</i>	(1)																																				
1.1.2	$\sqrt{-4}$	✓ Answer / <i>antwoord</i>	(1)																																				
1.2	<table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td>2</td><td>147</td><td></td><td></td></tr> <tr><td>2</td><td>73</td><td>r</td><td>1</td></tr> <tr><td>2</td><td>36</td><td>r</td><td>1</td></tr> <tr><td>2</td><td>18</td><td>r</td><td>0</td></tr> <tr><td>2</td><td>9</td><td>r</td><td>0</td></tr> <tr><td>2</td><td>4</td><td>r</td><td>1</td></tr> <tr><td>2</td><td>2</td><td>r</td><td>0</td></tr> <tr><td>2</td><td>1</td><td>r</td><td>0</td></tr> <tr><td></td><td>0</td><td>r</td><td>1</td></tr> </table> <p>$\therefore 147_{10} = 10010011_2$</p>	2	147			2	73	r	1	2	36	r	1	2	18	r	0	2	9	r	0	2	4	r	1	2	2	r	0	2	1	r	0		0	r	1	✓ Method / <i>metode</i> ✓ Answer / <i>antwoord</i> <div style="border: 1px solid black; padding: 5px; margin: 10px auto; width: fit-content;"> No mark awarded for answer if base NOT indicated. </div>	(2)
2	147																																						
2	73	r	1																																				
2	36	r	1																																				
2	18	r	0																																				
2	9	r	0																																				
2	4	r	1																																				
2	2	r	0																																				
2	1	r	0																																				
	0	r	1																																				
1.3.1	$\begin{array}{r} 1101 \\ \times 101 \\ \hline 1101 \\ 00000 \\ 110100 \\ \hline 1000001 \end{array}$ <table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td>2^6</td><td>2^5</td><td>2^4</td><td>2^3</td><td>2^2</td><td>2^1</td><td>2^0</td></tr> <tr><td>1</td><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td><td>1</td></tr> </table> $\begin{aligned} \therefore 1000001_2 &= (1 \times 2^0) + (0 \times 2^1) + (0 \times 2^2) \\ &\quad + (0 \times 2^3) + (0 \times 2^4) + (0 \times 2^5) \\ &\quad + (1 \times 2^6) \\ &= 1 + 64 \\ &= 65 \end{aligned}$	2^6	2^5	2^4	2^3	2^2	2^1	2^0	1	0	0	0	0	0	1	✓ Answer / <i>antwoord</i> ✓ Method / <i>metode</i> ✓ Answer / <i>antwoord</i>	(3)																						
2^6	2^5	2^4	2^3	2^2	2^1	2^0																																	
1	0	0	0	0	0	1																																	
1.3.2	$\begin{array}{r} {}^\circ 1100 r 11 \\ 101[111111 \\ \underline{101} \\ {}^\circ 101 \\ \underline{101} \\ {}^\circ \circ \circ 11 \end{array}$	✓ Answer / <i>antwoord</i> ✓ Method / <i>metode</i>	(2)																																				
1.4	$4,158 \times 10^{-6}$	✓ Answer / <i>antwoord</i>	(1)																																				
1.5	$x^2y^2 - 5xy + 4 = (-5)^2(2)^2 - 5(-5)(2) + 4 = 154$	✓ Substitution / <i>substitusie</i> ✓ Answer / <i>antwoord</i>	(2)																																				
			[12]																																				

QUESTION/VRAAG 2				
NO.	SOLUTION/OPLOSSING		EXPLANATION/ VERDUIDELIKING	
2.1	2.1.1	$(x - 2)(x^2 + 2x + 4)$ $= x^3 + 2x^2 + 4x - 2x^2 - 4x - 8$ $= x^3 - 8$	✓ Expand / <i>uitbreiding</i> ✓ Simplification / <i>vereenvoudiging</i>	(2)
	2.1.2	$3a(a - 8) + 3a^2 - 4(a - 1) - a^3$ $= 3a^2 - 24a + 3a^2 - 4a + 4 - a^3$ $= -a^3 + 6a^2 - 28a + 4$	✓ Expand / <i>uitbreiding</i> ✓ $-a^3$ ✓ $+6a^2$ ✓ $-28a$ ✓ $+4$	(5)
	2.1.3	$-2i(5 - 3i)$ $= -10i + 6i^2$ $= -10i + 6(-1)$ $= -10i - 6$ $= -6 - 10i$	✓ Expand / <i>uitbreiding</i> ✓ Substitution / <i>vervanging -1</i> ✓ Simplification / <i>vereenvoudiging</i>	(3)
2.2	2.2.1	$\frac{64^{x-1} \cdot 4^{2x+2}}{8^x}$ $= \frac{(2^6)^{x-1} \cdot (2^2)^{2x+2}}{(2^3)^x}$ $= \frac{2^{6x-6} \cdot 2^{4x+4}}{2^{3x}}$ $= \frac{2^{6x-6+4x+4}}{2^{3x}}$ $= \frac{2^{10x-2}}{2^{3x}}$ $= 2^{10x-2-3x}$ $= 2^{7x-2}$	 ✓ All prime factors correct / <i>alle priemfactore korrek</i> ✓ Exponent law / <i>Eksponent wet</i>	(3)
	2.2.2	$\frac{1}{x^2 - 4xy + 4y^2} + \frac{x^2 + 2xy + 4y^2}{x^3 - 8y^3} - \frac{1}{x^2 - 4y^2}$ $= \frac{1}{(x-2y)^2} + \frac{x^2 + 2xy + 4y^2}{(x-2y)(x^2 + 2xy + 4y^2)} - \frac{1}{(x-2y)(x+2y)}$ $= \frac{1}{(x-2y)^2} + \frac{1}{(x-2y)} - \frac{1}{(x-2y)(x+2y)}$ $= \frac{x+2y + (x-2y)(x+2y) - (x-2y)}{(x-2y)^2(x+2y)}$ $= \frac{x+2y + x^2 - 4y^2 - x + 2y}{(x-2y)^2(x+2y)}$ $= \frac{x^2 + 4y - 4y^2}{(x-2y)^2(x+2y)}$	✓ $(x-2y)^2$ ✓ $(x-2y)(x^2 + 2xy + 4y^2)$ ✓ $(x-2y)(x+2y)$ ✓ $\frac{1}{(x-2y)}$ ✓ Numerator / <i>teller</i> ✓ Denominator / <i>noemer</i> ✓ Simplification / <i>vereenvoudiging</i> ✓ Simplification / <i>vereenvoudiging</i>	(8)
			[21]	


QUESTION/VRAAG 3			
NO.	SOLUTION/OPLOSSING	EXPLANATION/ VERDUIDELIKING	
3.1	$3x^8 - 3$ $= 3(x^8 - 1)$ $= 3(x^4 - 1)(x^4 + 1)$ $= 3(x^2 - 1)(x^2 + 1)(x^4 + 1)$ $= 3(x - 1)(x + 1)(x^2 + 1)(x^4 + 1)$	✓ 3 common factor / <i>gemene faktor</i> ✓ $(x^4 - 1)(x^4 + 1)$ ✓ $(x^2 - 1)(x^2 + 1)(x^4 + 1)$ ✓ $3(x - 1)(x + 1)(x^2 + 1)(x^4 + 1)$	(4)
3.2	$x^2 - 5x + 6$ $= (x - 3)(x - 2)$	✓ $(x - 3)$ ✓ $(x - 2)$	(2)
3.3	$8x^3 - 27$ $= (2x - 3)(4x^2 + 6x + 9)$	✓ $(2x - 3)$ ✓ $(4x^2 + 6x + 9)$	(2)
			[8]



QUESTION/VRAAG 4				
NO.	SOLUTION/OPLOSSING		EXPLANATION/ VERDUIDELIKING	
4.1	4.1.1	$(x - 3)(4x + 20) = 0$ $x - 3 = 0$ or / of $4x + 20 = 0$ $x = 3$ $4x = -20$ $x = -5$	✓ $x = 3$ ✓ $x = -5$	(2)
	4.1.2	$\frac{4}{x-2} - \frac{10}{x} = \frac{2}{x^2 - 2x}$ $\frac{4}{x-2} - \frac{10}{x} = \frac{2}{x(x-2)}$ $\times x(x-2): 4x - 10(x-2) = 2$ $4x - 10x + 20 = 2$ $-6x = -18$ $x = 3$	✓ $x(x-2)$ ✓ Simplification / vereenvoudiging ✓ Answer / antwoord	(3)
	4.1.3	$81^{x-3} = \frac{1}{729}$ $(3^4)^{x-3} = 3^{-6}$ $3^{4x-12} = 3^{-6}$ $\therefore 4x - 12 = -6$ $4x = 6$ $x = \frac{6}{4} = \frac{3}{2}$	✓ 3^4 & 3^{-6} ✓ Exponent Law / eksponent wet ✓ Equation exponents / Gelykstelling van eksponente ✓ Answer / antwoord	(4)
4.2	$-\frac{2}{3}(7x - 2) < 6$ $\frac{-14}{3}x + \frac{4}{3} < 6$ $\times 3: -14x + 4 < 18$ $-14x < 14$ $x > -1$ 		✓ Expand / uitbreiding ✓ Simplification / vereenvoudiging ✓ Answer / antwoord ✓ Diagram / diagram <p style="text-align: center;">OR/OF</p>	
	$-\frac{2}{3}(7x - 2) < 6$ $7x - 2 < 6 \times -\frac{3}{2}$ $7x - 2 < -9$ $7x < -7$ $x > -1$ 			

4.3	$\frac{1}{b} + \frac{2b}{x} = 2$ $\frac{x + 2b^2}{bx} = 2$ $x + 2b^2 = 2bx$ $2b^2 = 2bx - x$ $2b^2 = x(2b - 1)$ $\frac{2b^2}{2b - 1} = x$ <p style="text-align: center;">OR/OF</p> $\frac{1}{b} + \frac{2b}{x} = 2$ $\frac{2b}{x} = 2 - \frac{1}{b}$ $\frac{2b}{x} = \frac{2b - 1}{b}$ $\frac{2b}{x} = \frac{2b - 1}{b}$ $2b^2 = 2bx - x$ $2b^2 = x(2b - 1)$ $\frac{2b^2}{2b - 1} = x$	$\checkmark \frac{x+2b^2}{bx}$ $\checkmark 2b^2 = x(2b - 1)$ $\checkmark \text{Answer / antwoord}$ <p style="text-align: center;">OR/OF</p> $\checkmark \frac{2b}{x} = \frac{2b-1}{b}$ $\checkmark \frac{x}{2b} = \frac{b}{2b-1} \text{ or/of}$ $x(2b-1) = 2b^2$ $\checkmark \text{Answer / antwoord}$	(3)
4.4	<p>Number of adults = x Number of children = y $x + y = 2200 \dots (1)$ $40x + 15y = 50500 \dots (2)$ $x = 2200 - y \dots 3$ Sub (3) into (2): $40(2200 - y) + 15y = 50500$ $88000 - 40y + 15y = 50500$ $-25y = -37500$ $y = 1500$ Sub $y = 1500$ in (3): $x = 2200 - 1500$ $x = 700$ $\therefore 1\ 500$ children and 700 adults</p> <p style="text-align: center;">OR/OF</p> $x + y = 2200 \dots (1)$ $40x + 15y = 50500 \dots (2)$ $\therefore y = 2200 - x \dots (3)$ Sub (3) into (2) $40x + 15(2200 - x) = 50500$ $40x + 33000 - 15x = 50500$ $25x = 17500$ $x = 700$ Sub $x = 700$ into (3) $y = 1500$ $\therefore 1500$ children and 700 adults / $1\ 500$ kinders en 700 volwassenes	 $\checkmark \checkmark \text{Setting up equation / opstel van vergelykings}$ $\checkmark \text{Substitution / vervanging}$ $\checkmark \text{Answer for } y \text{ / antwoord vir } y$ $\checkmark \text{Answer for } x \text{ / antwoord vir } x$	(5)
			[21]

QUESTION/VRAAG 5			
NO.	SOLUTION/OPLOSSING		EXPLANATION/ VERDUIDELIKING
5.1	$A = P(1 + i)^n$ $A = 7\,440(1 + 5,75\%)^8$ $A = R11\,636,33$		✓ Correct formula / <i>korrekte formule</i> ✓ Substitution into correct formula / <i>vervanging in korrekte formule</i> ✓ Answer / <i>antwoord</i>
5.2	5.2.1	Deposit / <i>deposito</i> = $R8\,000 \times 22\%$ $= R1\,760$ \therefore Principal amount / <i>begin waarde</i> $= R8\,000 - R1\,760$ $= R6\,240$	✓ Answer / <i>antwoord</i> ✓ Method / <i>metode</i> ✓ Answer / <i>antwoord</i>
	5.2.2	$A = P(1 + in)$ $A = 6\,240(1 + (10\%)(1))$ $A = R6\,864,00$	✓ Substitution into correct formula / <i>vervanging in korrekte formule</i> ✓ Answer / <i>antwoord</i>
	5.2.3	Monthly installment / <i>maandelikse betaling</i> $= R6\,864 \div 12$ $= R572$	✓ Method / <i>metode</i> ✓ Answer / <i>antwoord</i>
	5.2.4	$Total = R6\,864 + R1\,760$ $= R8\,624$	✓ Method / <i>metode</i> ✓ Answer / <i>antwoord</i>
5.3	$A = P(1 + i)^n$ $A = R24,99(1 + 15\%)^5$ $A = R50,26$		✓ Correct formula / <i>korrekte formule</i> ✓ Substitution into correct formula / <i>vervanging in korrekte formule</i> ✓ Answer / <i>antwoord</i>
			[15]

QUESTION/VRAAG 6			
NO.	SOLUTION/OPLOSSING	EXPLANATION/ VERDUIDELIKING	
6.1		<p>$h(x)$:</p> <ul style="list-style-type: none"> ✓ Shape / vorm ✓ Quadrants / kwadrante ✓ x- and y- intercepts / x- en y- afsnitte <p>$p(x)$:</p> <ul style="list-style-type: none"> ✓ Shape / vorm ✓ y-intercept / y-afsnit 	(5)
6.2.1 a)	$m = \frac{\Delta y}{\Delta x} = \frac{0 - 3}{0 - 2} = \frac{-3}{-2} = \frac{3}{2}$ $c = 3$	<ul style="list-style-type: none"> ✓ method / metode ✓ $m = \frac{3}{2}$ ✓ $c = 3$ 	(3)
6.2.1 b)	$b = 7$	✓ answer / antwoord	(1)
6.2.1 c)	Substitute any of the points A or D into $f(x)$ to calculate a $0 = a(-2)^2 + 7$ $0 = 4a + 7$ $-7 = 4a$ $\frac{7}{4} = a$ OR/OF $0 = a(2)^2 + 7$ $0 = 4a + 7$ $-7 = 4a$ $\frac{7}{4} = a$	 <ul style="list-style-type: none"> ✓ Substituting / vervanging ✓ Simplification / vereenvoudiging ✓ $-\frac{7}{4} = a$ 	(3)
6.2.2	$EB = 7 - 3$ $= 4 \text{ units / eenhede}$	<ul style="list-style-type: none"> ✓ Method / metode ✓ Answer / antwoord 	(2)
6.2.3	$x = 0$	✓ Answer / antwoord	(1)
6.2.4(a)	$m_{q(x)} \times m_{g(x)} = -1$ $m_{q(x)} \times \frac{3}{2} = -1$ $m_{q(x)} = -\frac{2}{3}$	✓ $m_{q(x)} = -\frac{2}{3}$	(1)

6.2.4(b)	$q(x) = -\frac{2}{3}x + c$ $(2; 0): \quad 0 = -\frac{2}{3}(2) + c$ $0 = -\frac{4}{3} + c$ $\frac{4}{3} = c$ $\therefore q(x) = -\frac{2}{3}x + \frac{4}{3}$	✓ Substituting / <i>vervanging</i> ✓ $\frac{4}{3} = c$ ✓ Equation / <i>vergelyking</i>	(3)
6.2.5	$-2 \leq x \leq \frac{8}{7}$	✓ interval notation / <i>notasie</i> ✓ endpoints / <i>eindpunte</i>	(2)
6.2.6	$x > 2$ or / <i>of</i> $x < -2$	✓ $x < -2$ ✓ $x > 2$	(2)
			[23]
TOTAL/TOTAAL:			100

