



**education**

Department:  
Education  
PROVINCE OF KWAZULU-NATAL

**NATIONAL  
SENIOR CERTIFICATE**

**GRADE 12**

**MATHEMATICS P2  
PREPARATORY EXAMINATION  
SEPTEMBER 2020**

**MARKS: 150**

**TIME: 3 hours**

**This question paper consists of 11 pages and an information sheet.**

**INSTRUCTIONS AND INFORMATION**

Read the following instructions carefully before answering the questions:

1. This question paper consists of **10** questions.
2. Answer **ALL** the questions.
3. Clearly show **ALL** calculations, diagrams, graphs, et cetera, which you have used in determining the answers.
4. Answers only will not necessarily be awarded full marks.
5. You may use an approved scientific calculator (non-programmable and non-graphical), unless stated otherwise.
6. If necessary, round off answers to **TWO** decimal places, unless stated otherwise.
7. Diagrams are **NOT** necessarily drawn to scale.
8. Number the answers correctly according to the numbering system used in this question paper.
9. Write neatly and legibly.

**QUESTION 1**

The total number of red cards issued per country to players during a soccer competition are given in the table below:

NUMBER OF RED CARDS	NUMBER OF COUNTRIES ( $f$ )	MIDPOINT OF INTERVAL ( $x$ )	$f \cdot x$
$0 < x \leq 2$	27		
$2 < x \leq 4$	15		
$4 < x \leq 6$	5		
$6 < x \leq 8$	5		
$8 < x \leq 10$	3		
<b>TOTAL</b>			

- 1.1 Calculate the estimated mean of the number of red cards per country. (3)
- 1.2 Draw an ogive curve to represent the above data. (3)
- 1.3 Calculate the interquartile range of the number of red cards issued per country in the competition. (2)
- [8]**

**QUESTION 2**

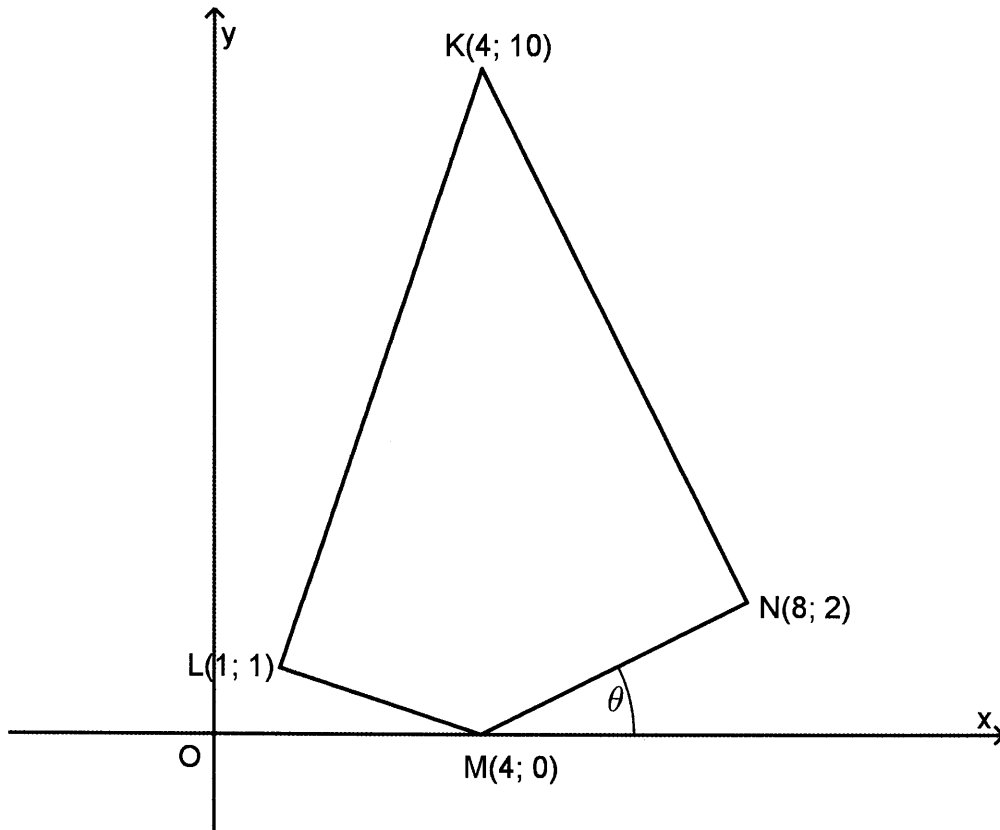
The table below shows a relationship between the monthly rent ( $x$ ) a person pays for an apartment and the person's monthly income ( $y$ ). Both are given in thousands of rands.

YEAR	2003	2004	2005	2006	2007	2008
Rent ( $x$ )	2	3	3,5	5,2	5,6	6
Income ( $y$ )	9	13,5	15	16,5	17	20

- 2.1 Determine the equation of the regression line. (4)
- 2.2 Determine the estimated monthly income if the rent per month is R9000. (2)
- 2.3 Calculate the value of the correlation coefficient. (2)
- 2.4 Describe the relationship between the monthly rent and the monthly income. (2)
- [10]**

**QUESTION 3**

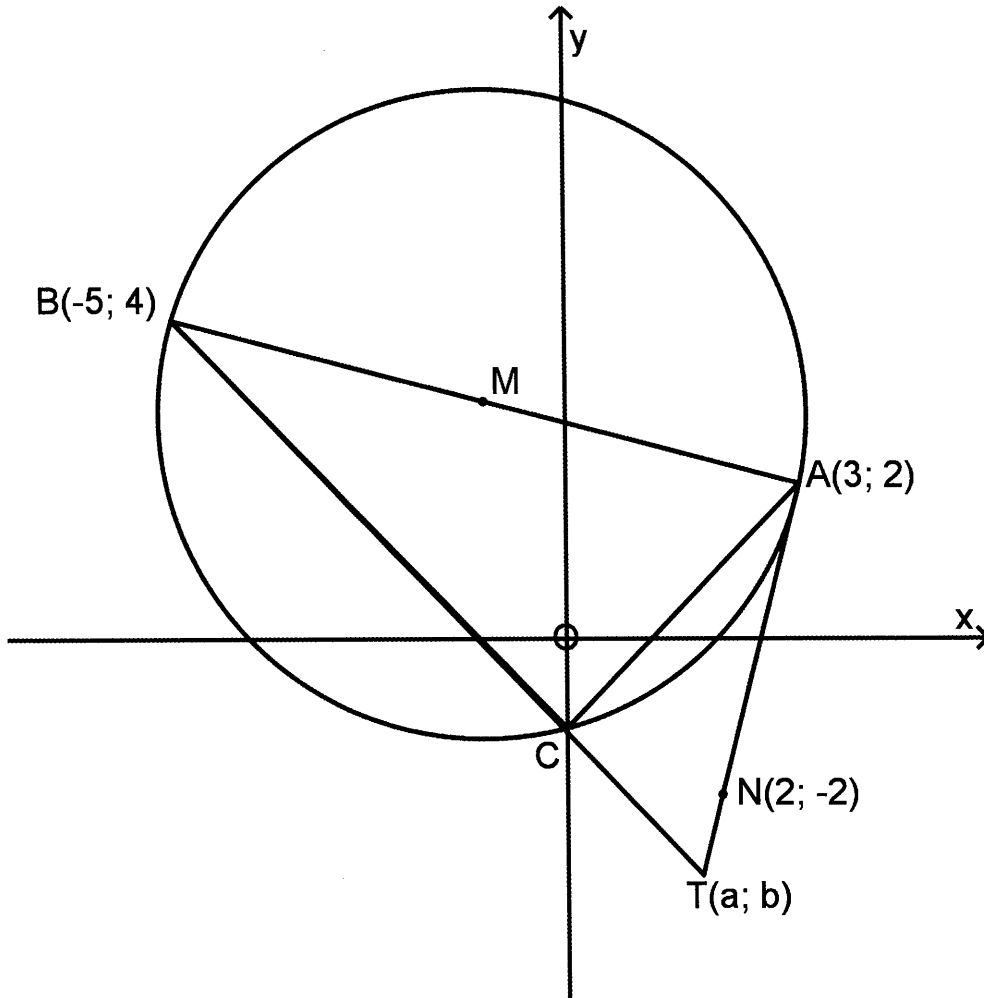
In the diagram KLMN is a quadrilateral with  $K(4; 10)$ ,  $L(1; 1)$ ,  $M(4; 0)$  and  $N(8; 2)$ .



- 3.1 Determine the:
- 3.1.1 gradient of LM and MN (4)
  - 3.1.2 length of KM. (2)
  - 3.1.3 value of  $\theta$  (2)
  - 3.1.4 midpoint of LN (2)
- 3.2 Show that  $KL \perp LM$  (3)
- 3.3 Prove that KLMN is a cyclic quadrilateral. (4)
- [17]**

**QUESTION 4**

In the sketch below, AB is a diameter with coordinates A(3; 2) and B(-5; 4) of circle ABC. M is the centre of the circle. BC produced meets AT in T. N(2; -2) is a point on the line TA. C is the y – intercept of the circle.



- 4.1 Determine the co-ordinates of M the centre of the circle (2)
- 4.2 Write down the equation of the circle in the form  $(x - p)^2 + (y - q)^2 = r^2$  (3)
- 4.3 Prove that TA is a tangent to the circle at A. (5)
- 4.4 Determine the equations of the lines
  - 4.4.1 TA and (4)
  - 4.4.2 BT (6)
- 4.5 If the coordinates of T are  $(a; b)$ , calculate the values of  $a$  and  $b$ . (3)

**[23]**

**QUESTION 5**

5.1 Without using a calculator, evaluate

$$\cos 79^\circ \cos 311^\circ + \sin 101^\circ \sin 49^\circ \quad (4)$$

5.2 Given:  $\sin(x + y) = 3 \sin(x - y)$

Prove that:  $\tan x = 2 \tan y \quad (4)$

5.3 Given:  $\frac{\cos x}{\sin 2x} - \frac{\cos 2x}{2 \sin x} = \sin x$

5.3.1 Prove that  $\frac{\cos x}{\sin 2x} - \frac{\cos 2x}{2 \sin x} = \sin x \quad (4)$

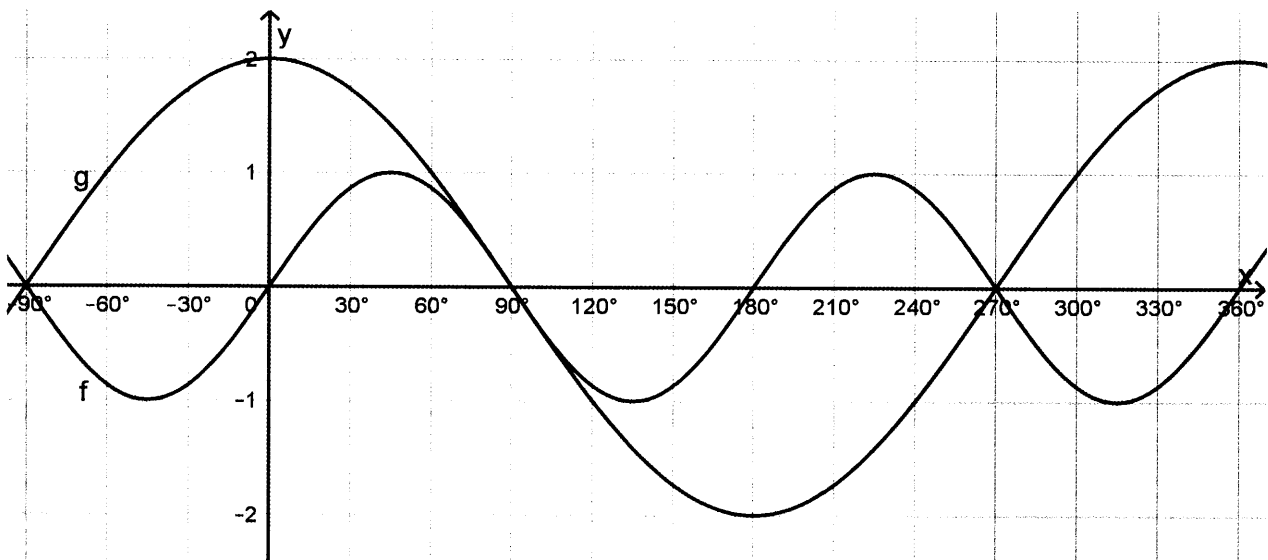
5.3.2 Hence, solve for  $x$  where  $x \in [0^\circ; 360^\circ]$ :

$$1 + 2 \cos 2x = \frac{\cos 2x}{2 \sin x} - \frac{\cos x}{\sin 2x} \quad (6)$$

[18]

**QUESTION 6**

In the diagram, the graphs of  $f(x) = a \sin bx$  and  $g(x) = c \cos dx$  are drawn for the interval  $x \in [-90^\circ; 360^\circ]$



6.1 Determine the values of  $a$ ,  $b$ ,  $c$  and  $d$ . (4)

6.2 Write down the period of  $g$ . (1)

6.3 Determine the value(s) of  $x$  in the interval  $x \in [-90^\circ; 360^\circ]$ , for which

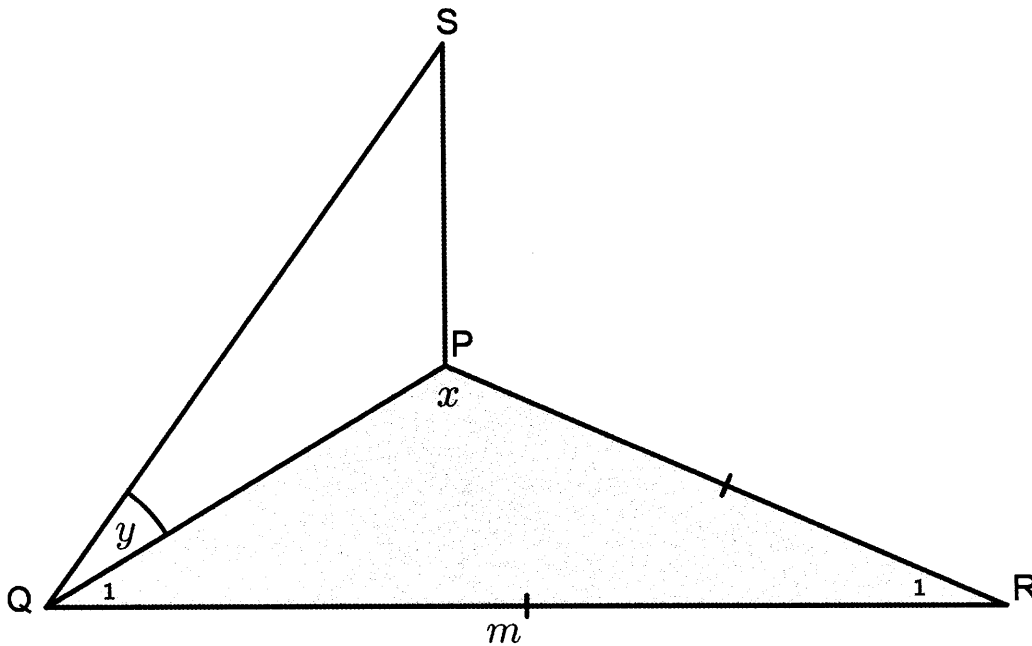
6.3.1  $f(x) \leq g(x) \quad (2)$

6.3.2  $f'(x) \times g'(x) > 0$  where  $g(x) > 0 \quad (3)$

[10]

**QUESTION 7**

In the diagram P, Q and R are three points in the same horizontal plane.  $PR = QR = m$ ,  $\hat{QPR} = x$ . SP is perpendicular to PQ. The angle of elevation of S from Q is  $y$ .

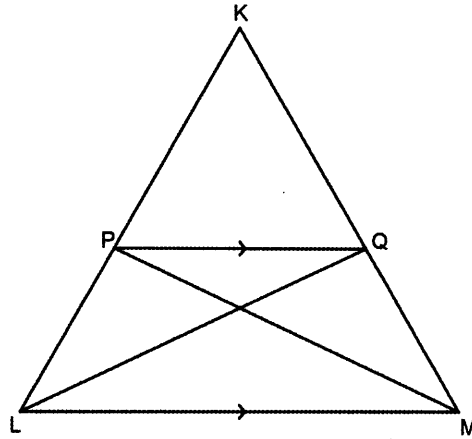


- 7.1 Express the area of  $\Delta PQR$  in terms of  $x$  and  $m$ . (5)
- 7.2 Show that  $PQ = 2m \cos x$  (4)
- 7.3 Hence, prove that  $SP = 2m \cos x \tan y$  (2)

[11]

**QUESTION 8**

- 8.1 In the diagram below  $\triangle KLM$  is given, with P and Q lying on KL and KM respectively such that  $PQ \parallel LM$ . PM and LQ are drawn.



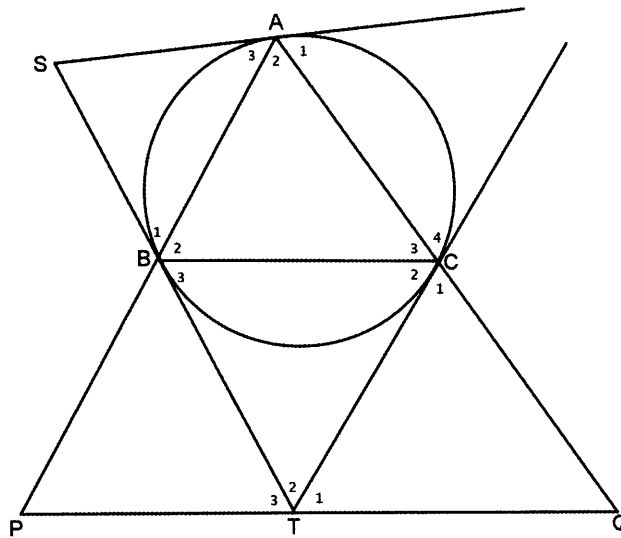
Prove that  $\frac{KP}{PL} = \frac{KQ}{QM}$

(6)



8.2 In the diagram, SBT, SA and TC are tangents to the circle at B, A and C respectively. AB is produced to P and AC is produced to Q such that T lies on the line PQ.

In  $\triangle APQ$ ,  $\frac{AB}{AP} = \frac{AC}{AQ}$ .



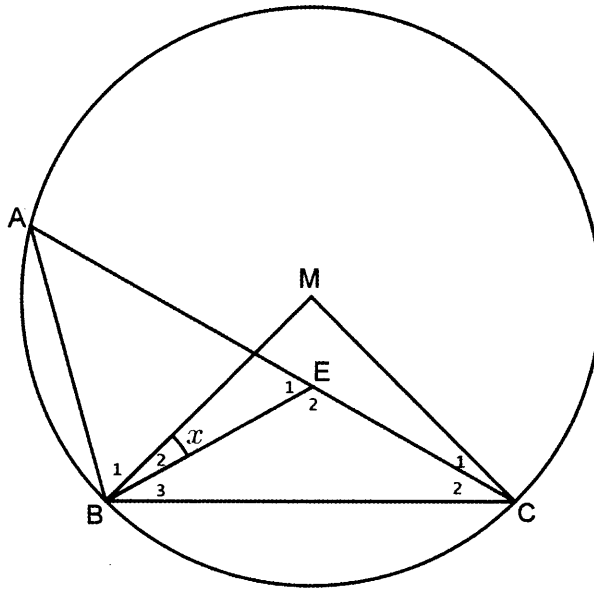
Use the above information to prove:

- 8.2.1  $\hat{A}_2 = \hat{T}_1$  (4)
- 8.2.2  $\triangle ABC \parallel \triangle TCQ$  (4)
- 8.2.3 ABTQ is a cyclic quadrilateral. (4)
- 8.2.4 Prove that TQ is a tangent to circle TBC at T. (5)

[23]

**QUESTION 9**

In the diagram, M is the centre of the circle through A, B and C. E is on AC. AC bisects  $\widehat{MCB}$  and EB bisects  $\widehat{MBC}$ .  $\widehat{B}_2 = x$



9.1 Determine the size of  $\widehat{E}_2$  in terms of  $x$ . (4)

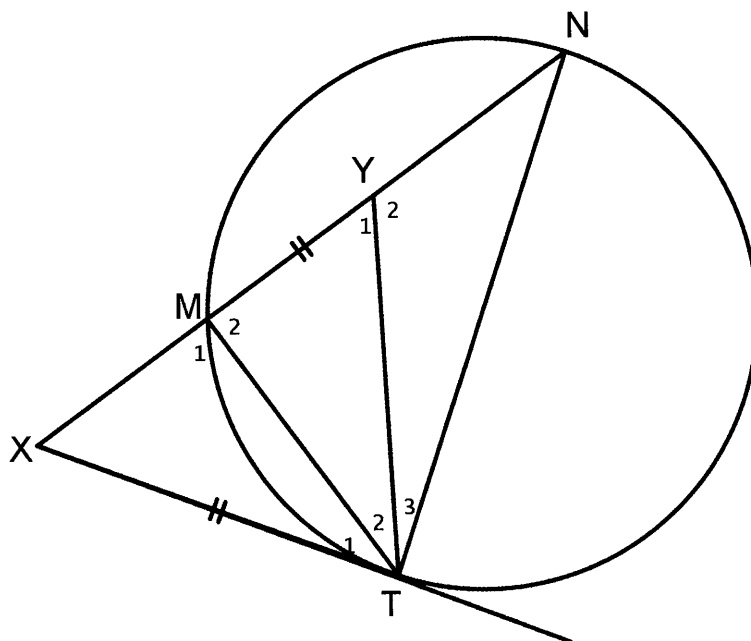
9.2 Show  $\widehat{BAC} = 90^\circ - 2x$  (3)

9.3 Prove that AE is a diameter of circle ABE. (5)

**[12]**

**QUESTION 10**

10.1 In the diagram XMN is a straight line and XT is a tangent to the circle. Y is a point on XN so that XY = YT.



Prove that:

10.1.1 YT bisect  $\hat{MTN}$ . (5)

10.1.2  $\frac{XM}{XT} = \frac{XT}{XN}$  (6)

10.2 Given that MY = 20 mm, YN = 50 mm and XT = k mm:

10.2.1 Express XM in terms of k. (3)

10.2.2 Calculate the length of k. (4)

[18]

**TOTAL MARKS: 150**

**INFORMATION SHEET: MATHEMATICS**

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$A = P(1 + ni)$$

$$A = P(1 - ni)$$

$$A = P(1 - i)^n$$

$$A = P(1 + i)^n$$

$$T_n = a + (n - 1)d$$

$$S_n = \frac{n}{2}(2a + (n - 1)d)$$

$$T_n = ar^{n-1}$$

$$S_n = \frac{a(r^n - 1)}{r - 1}; \quad r \neq 1$$

$$S_\infty = \frac{a}{1 - r}; \quad -1 < r < 1$$

$$F = \frac{x[(1 + i)^n - 1]}{i}$$

$$P = \frac{x[1 - (1 + i)^{-n}]}{i}$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x + h) - f(x)}{h}$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$M\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$$

$$y = mx + c$$

$$y - y_1 = m(x - x_1)$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \tan \theta$$

$$(x - a)^2 + (y - b)^2 = r^2$$

$$\text{In } \triangle ABC: \quad \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cdot \cos A$$

$$\text{area } \triangle ABC = \frac{1}{2} ab \cdot \sin C$$

$$\sin(\alpha + \beta) = \sin \alpha \cdot \cos \beta + \cos \alpha \cdot \sin \beta$$

$$\sin(\alpha - \beta) = \sin \alpha \cdot \cos \beta - \cos \alpha \cdot \sin \beta$$

$$\cos(\alpha + \beta) = \cos \alpha \cdot \cos \beta - \sin \alpha \cdot \sin \beta$$

$$\cos(\alpha - \beta) = \cos \alpha \cdot \cos \beta + \sin \alpha \cdot \sin \beta$$

$$\cos 2\alpha = \begin{cases} \cos^2 \alpha - \sin^2 \alpha \\ 1 - 2\sin^2 \alpha \\ 2\cos^2 \alpha - 1 \end{cases}$$

$$\sin 2\alpha = 2 \sin \alpha \cdot \cos \alpha$$

$$\bar{x} = \frac{\sum f \cdot x}{n}$$

$$\sigma^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n}$$

$$P(A) = \frac{n(A)}{n(S)}$$

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

$$\hat{y} = a + bx$$

$$b = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sum (x - \bar{x})^2}$$



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**MATHEMATICS P2**

**PREPARATORY EXAMINATION**

**SEPTEMBER 2020**

**SPECIAL ANSWER BOOK**

**NATIONAL  
SENIOR CERTIFICATE**

**GRADE 12**

NAME OF CANDIDATE: \_\_\_\_\_

150

TIME: 3 hours

This answer book consists of 20 pages

**QUESTION 1**

NUMBER OF RED CARDS	NUMBER OF COUNTRIES ( $f$ )	MIDPOINT OF INTERVAL ( $x$ )	$f \cdot x$
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$6 < x \leq 8$	5		
$8 < x \leq 10$	3		
<b>TOTAL</b>			

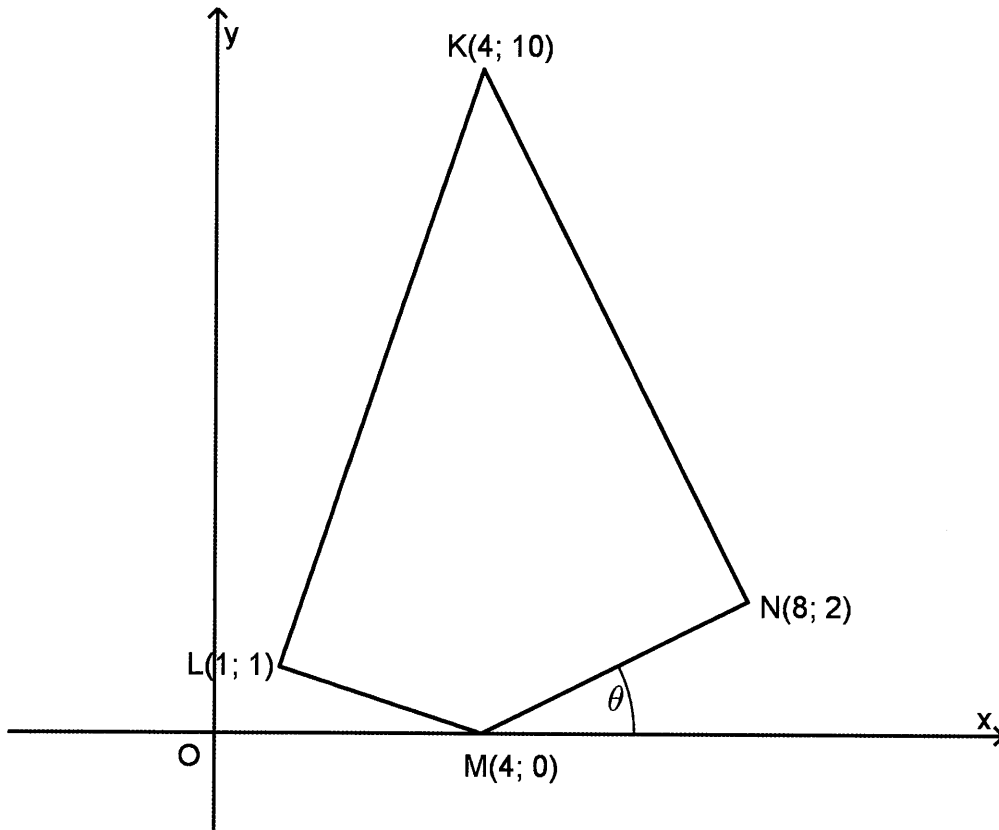
	Solution/ <i>Oplossing</i>	Marks/ <i>Punte</i>
1.1		(3)
1.2	<p style="text-align: center;"><b>The red cards issued to countries during a soccer competition</b></p>	(3)
1.3		(2)
		<b>[8]</b>

**QUESTION 2**

YEAR	2003	2004	2005	2006	2007	2008
Rent ( $x$ )	2	3	3,5	5,2	5,6	6
Income ( $y$ )	9	13,5	15	16,5	17	20

	<i>Solution/Oplissing</i>	<i>Marks/ Punte</i>
2.1		(4)
2.2		(2)
2.3		(2)
2.4		(2)
		<b>[10]</b>

**QUESTION 3**

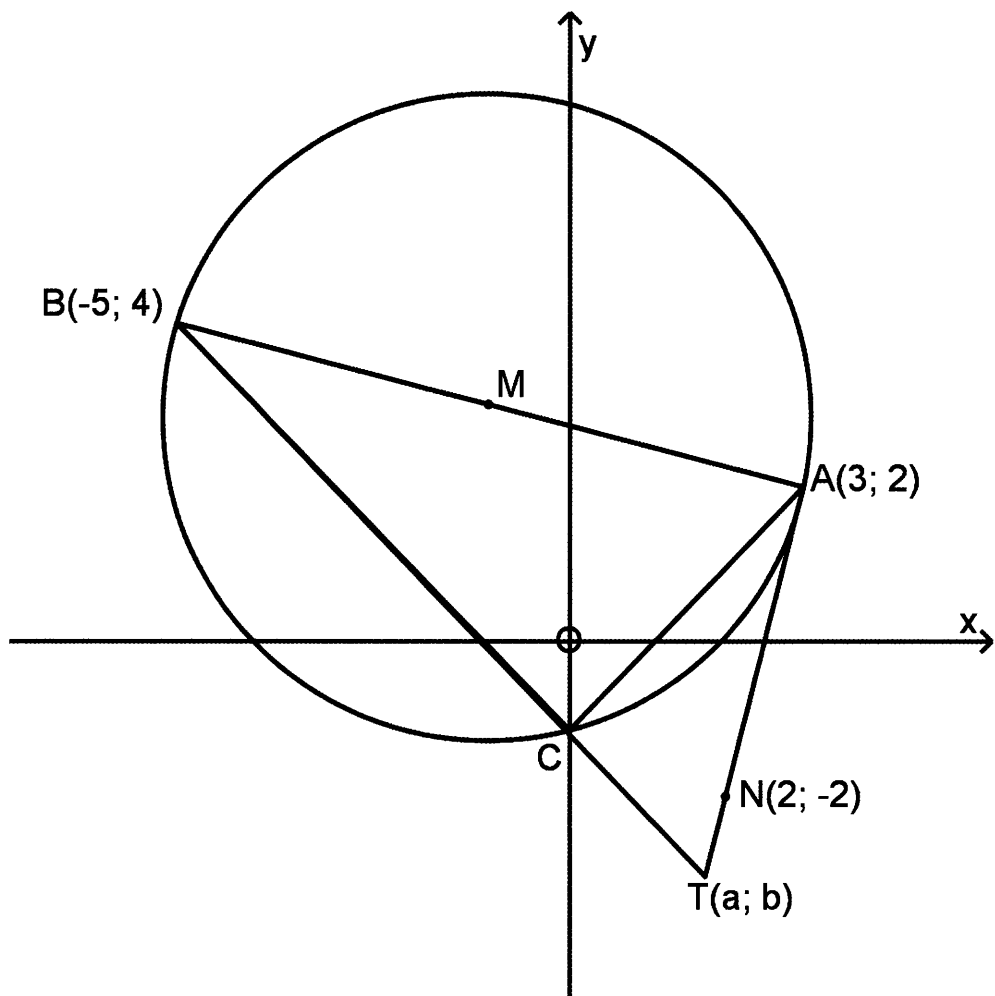


	<b>Solution/Oplissing</b>	<b>Marks/Punte</b>
3.1.1		(4)
3.1.2		(2)



	Solution/ <i>Oplossing</i>	Marks/ <i>Punte</i>
3.1.3		(2)
3.1.4		(2)
3.2		(3)
3.3		(4)
		<b>[17]</b>

**QUESTION 4**



	<i>Solution/Oplissing</i>	<i>Marks/Punte</i>
4.1		(2)
4.2		(3)

	<b>Solution/Oplossing</b>	<b>Marks/ Punte</b>
4.3		(5)
4.4.1		(4)
4.4.2		(6)

	<b>Solution/Oplissing</b>	<b>Marks/ Punte</b>
4.5		(3)
		<b>[23]</b>

**QUESTION 5**

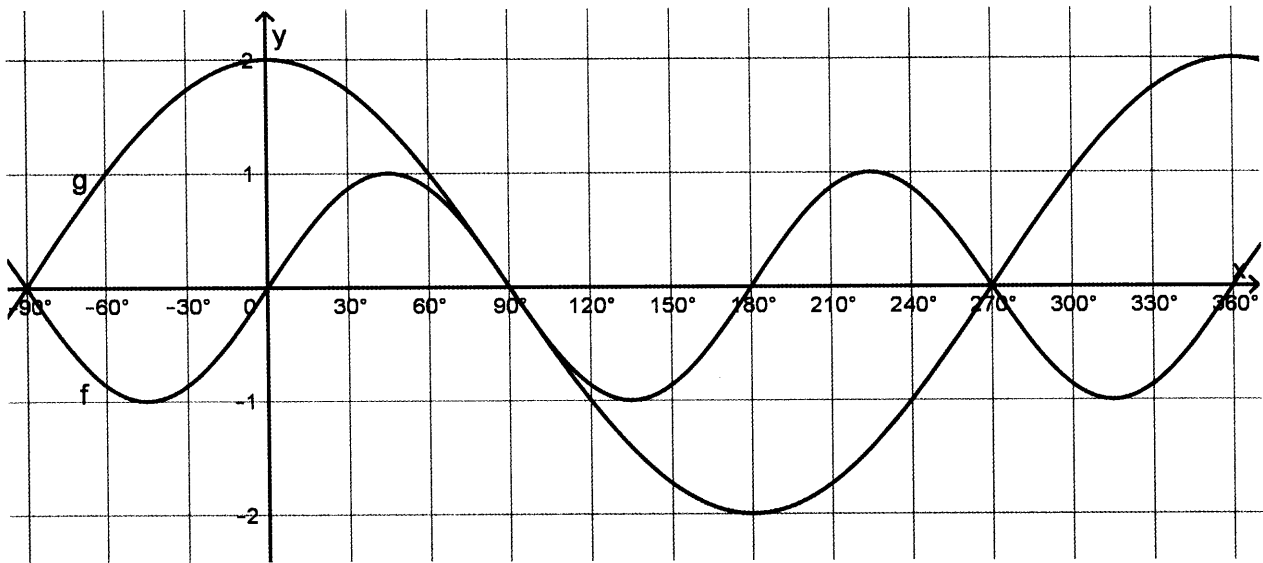
	<b>Solution/Oplissing</b>	<b>Marks/ Punte</b>
5.1		(4)
5.2		

	<b>Solution/Oplossing</b>	<b>Marks/ Punte</b>
5.2 (CONT)		(4)
5.3.1		(4)

	<i>Solution/Oplissing</i>	<i>Marks/ Punte</i>
5.3.2		(6)

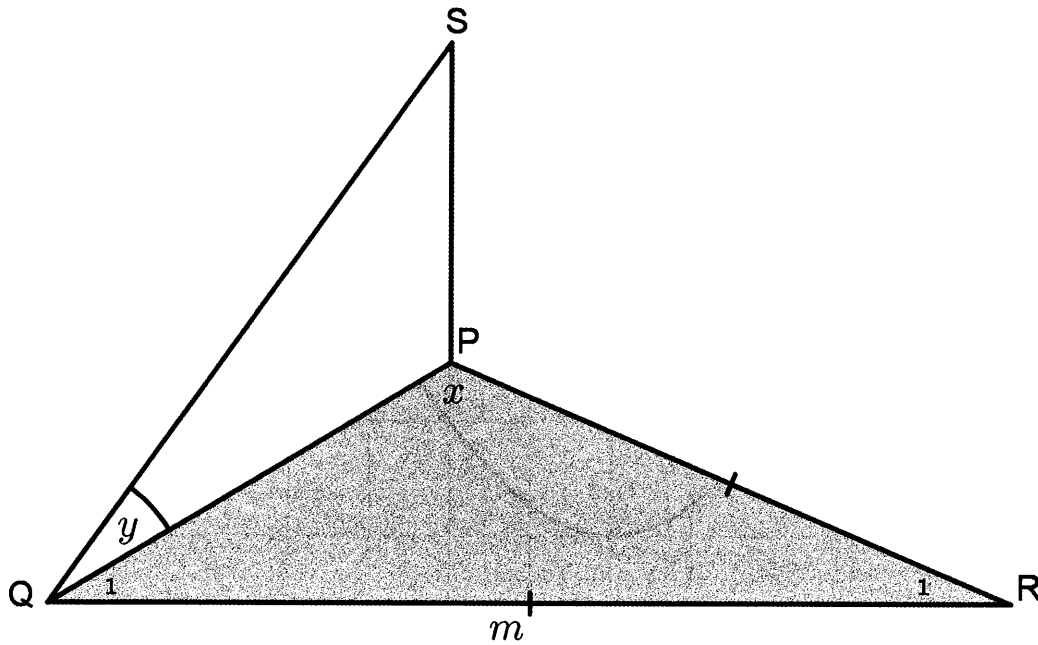
<i>Additional space/Bykomende ruimte</i>

**QUESTION 6**



	<i>Solution/Oplissing</i>	<i>Marks/Punte</i>
6.1		(4)
6.2		(1)
6.3.1		(2)
6.3.2		(3)
		<b>[10]</b>

**QUESTION 7**

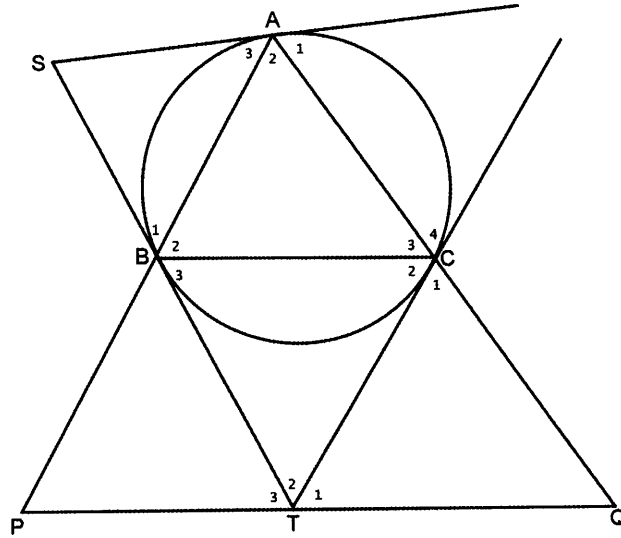


	<i>Solution/Oplossing</i>	<b>Marks/ Punte</b>
7.1		(5)



	<b>Solution/Oplossing</b>	<b>Marks/ Punte</b>
7.2		(4)
7.3		(2)
		<b>[11]</b>



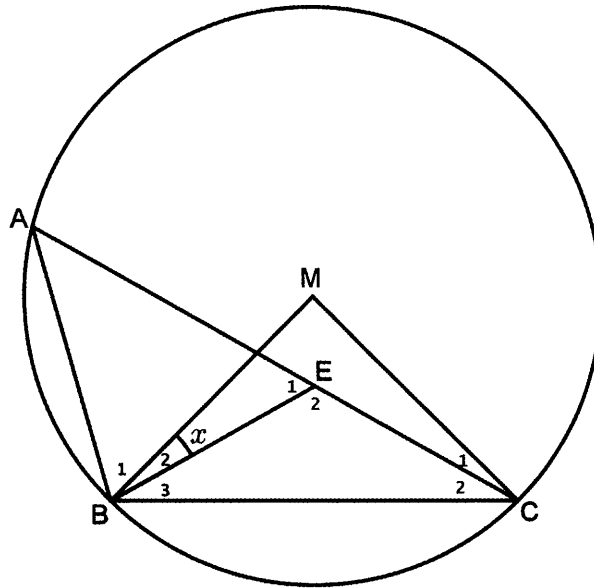


	<i>Solution/Oplissing</i>	<i>Marks/ Punte</i>
8.2.1		(4)
8.2.2		(4)

	<i>Solution/Oplissing</i>	<i>Marks/Punte</i>
8.2.3		(4)
8.2.4		(5)
		[23]

	<i>Additional space/Bykomende ruimte</i>	<i>Marks/Punte</i>

**QUESTION 9**



	<i>Solution/Oplissing</i>	<i>Marks/Punte</i>
9.1		(4)
9.2		(3)

	<i>Solution/Oplissing</i>	<i>Marks/Punte</i>
9.3		(5)
		[12]

**QUESTION 10**

	<i>Solution/Oplissing</i>	<i>Marks/Punte</i>
10.1.1		
		(5)

	<i>Solution/Oplissing</i>	<i>Marks/Punte</i>
10.1.2		
		(6)
10.2.1		
		(3)
10.2.2		
		(4)
		<b>[18]</b>

**TOTAL: 150**







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**GRADE 12**

**MATHEMATICS P2  
PREPARATORY EXAMINATION  
SEPTEMBER 2020  
MARKING GUIDLINES**

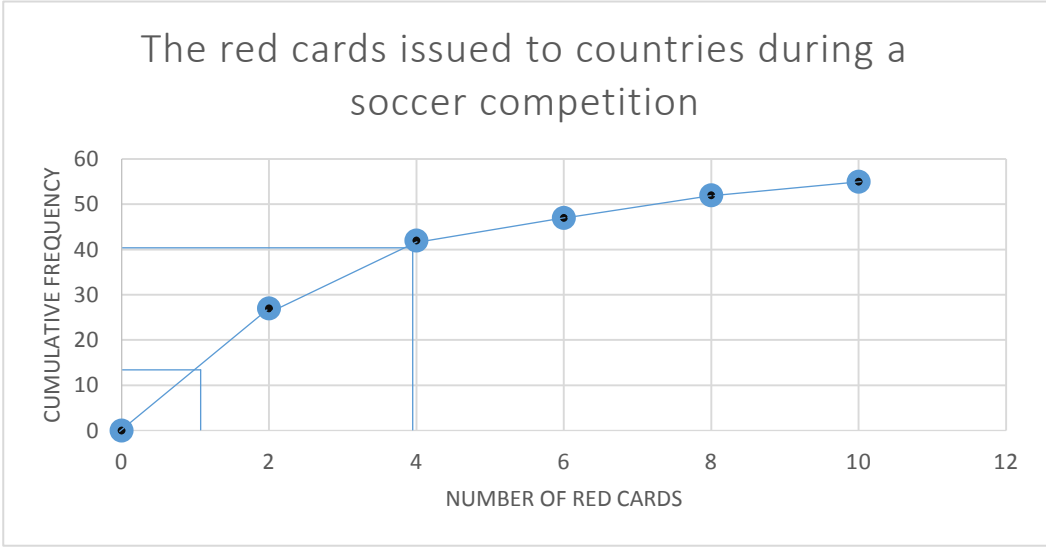
**MARKS: 150**

**TIME: 3 hours**

**This marking guideline consists of 12 pages.**

**QUESTION 1**

NUMBER OF RED CARDS	NUMBER OF COUNTRIES ( <i>f</i> )	MIDPOINT OF INTERVAL ( <i>x</i> )	<i>f</i> · <i>x</i>
$0 < x \leq 2$	27	1	27
$2 < x \leq 4$	15	3	45
$4 < x \leq 6$	5	5	25
$6 < x \leq 8$	5	7	35
$8 < x \leq 10$	3	9	27
<b>TOTAL</b>	55		159

1.1	Estimated mean = $\frac{159}{55} = 2,89 \approx 3$ red cards  Answer only full marks	CA ✓ 159 CA ✓ 55 CA ✓ answer (3)
1.2	<p style="text-align: center;">The red cards issued to countries during a soccer competition</p> 	✓✓✓ Full marks for 6 correct points  ✓✓2 marks for 4 correct points  ✓1 mark for 2 correct points  (3)
1.3	$Q_3 = 4$ and $Q_1 = 1 \therefore IQR = 4 - 1 = 3$ red cards  Answer only full marks	CA ✓ $Q_1$ and $Q_3$ CA ✓ answer (2)
<b>[8]</b>		

## QUESTION 2

2.1	$A = 5,97$ ; $B = 2,18$ $Y = 5,97 + 2,18x$  Answer only full marks	A ✓ for A A ✓ for B A ✓✓ For equation (4)
2.2	Estimated monthly income $y = 5,97 + 2,18(9)$ $= 25,59$ $\therefore$ Monthly income = R25598,89 If 9000 is used only 1 mark	CA ✓ substitution CA ✓ answer (2)
2.3	$r = 0,94$	CA ✓✓ (2)
2.4	Very strong positive relationship between the monthly rent and the monthly income.	CA ✓ strong CA ✓ positive (2)
<b>[10]</b>		



**QUESTION 3**


3.1.1	$m_{LM} = \frac{0 - 1}{4 - 1} = -\frac{1}{3}$ $m_{MN} = \frac{2 - 0}{8 - 4} = \frac{1}{2}$	A✓ sub into correct formula A ✓ $-\frac{1}{3}$  A✓ Sub into correct formula A ✓ $\frac{1}{2}$  (4)
3.1.2	$KM = \sqrt{(4-4)^2 + (10-0)^2}$ $= \sqrt{100}$ $= 10 \text{ units}$ Answer only full marks	CA ✓ subst  CA ✓ 10 units  (2)
3.1.3	$m_{MN} = \frac{1}{2}$ $\tan \theta = \frac{1}{2}$ $\theta = 26,57^\circ$ Answer only full marks	CA ✓ $\tan \theta = \frac{1}{2}$  CA ✓ $\theta = 26,57^\circ$ provided acute angle (2)
3.1.4	$\left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$ $\left( \frac{1+8}{2}, \frac{1+2}{2} \right)$ $\left( \frac{9}{2}, \frac{3}{2} \right)$	A✓ correct substitution    A✓ answer (2)
3.2	$m_{KL} = \frac{10 - 1}{4 - 1} = 3$ $m_{KL} \times m_{LM} = 3 \times \left(-\frac{1}{3}\right)$ $= -1$ $\therefore KL \perp LM$	A✓ subst  A✓ 3  A✓ product = -1  (3)
3.3	$m_{KN} = \frac{10 - 2}{4 - 8}$ $= -2$ $\therefore KN \perp NM$ $\therefore \hat{KLM} + \hat{KNM} = 180^\circ$ $\therefore KLMN \text{ is cyclic quadrilateral (converse, opp } \angle^s \text{ of a cyclic quad are supplementary)}$	A✓ $m_{KN} = -2$  A✓ $KN \perp MN$ A✓ Sum of $180^\circ$ $m_{MN} = \frac{1}{2} \therefore (-2) \left(\frac{1}{2}\right) = -1$  A✓ reason  (4) <b>[17]</b>



**QUESTION 4**


4.1	$M\left(\frac{-5+3}{2}; \frac{4+2}{2}\right) = M(-1; 3)$	A✓ $x = -1$ A✓ $y = 3$ (2)
4.2	$r^2 = BM^2 = (-5+1)^2 + (4-3)^2 = 17$ $\therefore (x+1)^2 + (y-3)^2 = 17$	CA✓ subst into equation CA✓ $r^2 = 17$ CA✓ equation For CA marks coordinates of M must be in second quadrant (3)
4.3	$m_{AB} = \frac{2-3}{3+1} = -\frac{1}{4}$ $m_{AN} = \frac{2+2}{3-2} = 4$ $m_{AB} \times m_{AN} = -1$ $\therefore \hat{B}AT = 90^\circ$ $\therefore TA \text{ is a tangent (conv. tangent and diameter)}$	A✓ $m_{MA}$ or $m_{BA}$ A✓ $m_{AN}$ A✓ product of gradients = -1 A✓ $90^\circ$ A✓ reason (5)
4.4.1	$m_{TA} = m_{AN} = 4$ $y = 4x + c$ Subst. (3; 2): $2 = 4(3) + c$ $-10 = c$ $\therefore y = 4x - 10$	CA✓ $m_{TA} = m_{AN}$ CA✓ equation CA✓ subst of (3; 2) or (2; -2) CA✓ equation (4)
4.4.2	Let C(x; y) $\therefore (x+1)^2 + (y-3)^2 = 17$ At C; $x = 0$ $\therefore (0+1)^2 + (y-3)^2 = 17$ $(y-3)^2 = 16$ $y-3 = \pm 4$ $y = 7 \text{ or } y = -1$ $\therefore C(0; -1)$ $m_{BC} = \frac{-1-4}{0+5} = -1$ Now $y = -x - 1$	CA✓ equation of circle CA✓ subst $x = 0$ CA✓ y values CA✓ co-ordinate CA✓ gradient CA✓ equation (6)
4.5	Lines AT and BT intersect at C $\therefore 4x - 10 = -x - 1$ $5x = 9$ $x = \frac{9}{5} = a$ $b = -\frac{9}{5} - 1 = -2\frac{4}{5}$	CA✓ equations equal CA✓ value of a CA✓ value of b, For CA marks A and B are points in the 4 <sup>th</sup> quadrant (3)

**QUESTION 5**

<p>5.1</p>	$\begin{aligned} &\cos 79^\circ \cos 311^\circ + \sin 101^\circ \sin 49^\circ \\ &= \cos 79^\circ \cos 49^\circ + \sin 79^\circ \sin 49^\circ \\ &= \cos(79^\circ - 49^\circ) \\ &= \cos 30^\circ \\ &= \frac{\sqrt{3}}{2} \end{aligned}$ <p>Answer only no marks, used calculator</p>	<p>A✓ <math>\cos 49^\circ</math> A✓ <math>\sin 79^\circ</math></p> <p>A✓ <math>\cos 30^\circ</math></p> <p>A✓ answer</p> <p>(4)</p>
<p>5.2</p>	$\begin{aligned} \sin(x + y) &= 3 \sin(x - y) \\ \sin x \cos y + \cos x \sin y &= 3(\sin x \cos y - \cos x \sin y) \\ \sin x \cos y + \cos x \sin y &= 3 \sin x \cos y - 3 \cos x \sin y \\ -2 \sin x \cos y &= -4 \cos x \sin y \\ \div -2 \cos x \cos y: & \\ \frac{\sin x}{\cos x} &= 2 \left( \frac{\sin y}{\cos y} \right) \\ \therefore \tan x &= 2 \tan y \end{aligned}$	<p>A✓ expansion</p> <p>A✓ like terms added</p> <p>A✓ divide</p> <p>A✓</p> $\frac{\sin x}{\cos x} = 2 \left( \frac{\sin y}{\cos y} \right)$ <p>(4)</p>
<p>5.3.1</p>	$\frac{\cos x}{\sin 2x} - \frac{\cos 2x}{2 \sin x} = \sin x$ <p>LHS:</p> $\begin{aligned} &\frac{\cos x}{\sin 2x} - \frac{\cos 2x}{2 \sin x} \\ &= \frac{\cos x}{2 \sin x \cos x} - \frac{1 - 2 \sin^2 x}{2 \sin x} \\ &= \frac{1}{2 \sin x} - \frac{1 - 2 \sin^2 x}{2 \sin x} \\ &= \frac{1 - 1 + 2 \sin^2 x}{2 \sin x} \\ &= \frac{2 \sin^2 x}{2 \sin x} \\ &= \sin x \\ &= \text{RHS} \end{aligned}$	 <p>A✓ <math>2 \sin x \cos x</math></p> <p>A✓ <math>1 - 2 \sin^2 x</math></p> <p>A✓ numerator</p> <p>A✓ answer</p> <p>(4)</p>

5.3.2	$1 + 2 \cos 2x = \frac{\cos 2x}{2 \sin x} - \frac{\cos x}{\sin 2x}$ $1 + 2 \cos 2x = -\sin x$ $1 + 2(1 - 2\sin^2 x) = -\sin x$ $1 + 2 - 4\sin^2 x = -\sin x$ $4\sin^2 x - \sin x - 3 = 0$ $(\sin x - 1)(4 \sin x + 3) = 0$ $\sin x = 1 \qquad \text{OR} \qquad \sin x = -\frac{3}{4}$ $x = 90^\circ \qquad \text{ref} \angle = 48,59^\circ$ $x = 228,59$ $\text{OR}$ $x = 311,41^\circ$	<p>A✓ - sin x</p> <p>A✓ standard quadratic form</p> <p>A ✓ Factors</p> <p>CA✓90<sup>0</sup></p> <p>CA✓228.59°</p> <p>CA✓311.41°</p> <p>(6)</p>
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**QUESTION 6**

6.1	$a = 1$ $b = 2$ $c = 2$ $d = 1$	 <p>A✓ a = 1</p> <p>A✓ b = 2</p> <p>A✓ c = 2</p> <p>A✓ d = 1</p> <p>(4)</p>
6.2	360°	<p>A✓ 360°</p> <p>(1)</p>
6.3.1	$x \in [-90^\circ; 90^\circ]$ or $x \in [270^\circ; 360^\circ]$	<p>AA✓✓ values and notation</p> <p>(2)</p>
6.3.2	$x \in (-45^\circ; 0^\circ)$ or $x \in (45^\circ; 90^\circ)$ or $x \in (315^\circ; 360^\circ)$	<p>AAA✓✓✓ values and correct notation</p> <p>(3)</p>
<b>[11]</b>		

**QUESTION 7**

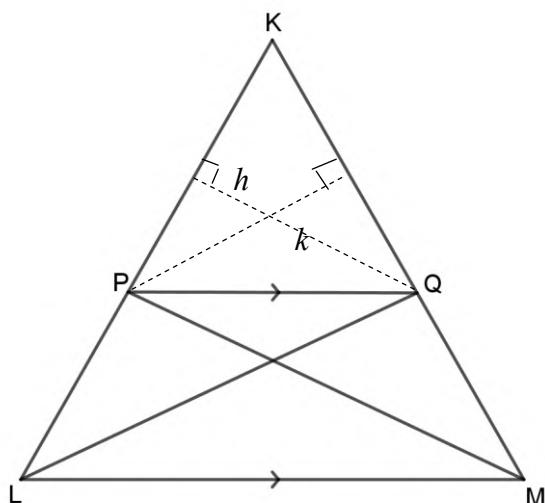
7.1	<p>In <math>\Delta PQR</math>:</p> $\hat{Q}_1 = x \quad (PR = QR)$ $\hat{R} = 180^\circ - 2x \quad (\text{sum of } \angle \Delta PQR)$ $\text{Area of } \Delta PQR = \frac{1}{2} pq \sin \hat{R}$ $= \frac{1}{2} m \cdot m \sin(180^\circ - 2x)$ $= \frac{1}{2} m^2 \sin 2x$	<p><math>A \checkmark \hat{Q}_1 = x</math>  <math>A \checkmark \hat{R} = 180^\circ - 2x</math>  <math>A \checkmark</math> Subst. into Area rule  <math>A \checkmark \sin 2x</math>  <math>A \checkmark</math> answer</p> <p style="text-align: right;">(5)</p>
7.2	$\therefore \frac{PQ}{\sin(180^\circ - 2x)} = \frac{m}{\sin x}$ $\therefore PQ = \frac{m \cdot \sin(180^\circ - 2x)}{\sin x}$ $\therefore PQ = \frac{m \cdot \sin 2x}{\sin x}$ $\therefore PQ = \frac{m \cdot 2 \sin x \cdot \cos x}{\sin x}$ $\therefore PQ = 2m \cos x$	<p><math>A \checkmark</math> Use of sine rule  <math>A \checkmark</math> subst into sine Rule  <math>A \checkmark \sin 2x</math>  <math>A \checkmark 2 \sin x \cos x</math>  (4)</p>
7.3	<p>In <math>\Delta SPQ</math>:</p> $\tan y = \frac{SP}{PQ}$ $\therefore SP = PQ \tan y$ $\therefore SP = 2m \cos x \tan y$	<p><math>A \checkmark \tan y = \frac{SP}{PQ}</math>  <math>A \checkmark SP = PQ \tan y</math></p> <p style="text-align: right;">(2)</p>






**QUESTION 8**

8.1



<p>R.T.P</p> $\frac{KP}{PL} = \frac{KQ}{QM}$ <p>CONSTRUCTION:</p> <p>In <math>\triangle KPQ</math>, draw perpendicular heights, <math>h</math> from <math>Q</math> to <math>KP</math> and <math>k</math> from <math>P</math> to <math>KQ</math></p> <div style="text-align: center;">  </div> $\frac{\text{Area of } \triangle KPQ}{\text{Area of } \triangle LPQ} = \frac{\frac{1}{2} KP \times h}{\frac{1}{2} PL \times h}$ $= \frac{KP}{PL}$ $\frac{\text{Area of } \triangle KPQ}{\text{Area of } \triangle MPQ} = \frac{\frac{1}{2} KQ \times k}{\frac{1}{2} QM \times k}$ $= \frac{KQ}{QM}$ <p>But area of <math>\triangle PLQ = \text{Area of } \triangle MPQ</math> Same base, same height</p> $\therefore \frac{\text{Area of } \triangle KPQ}{\text{Area of } \triangle LPQ} = \frac{\text{Area of } \triangle KPQ}{\text{Area of } \triangle MPQ}$ $\therefore \frac{KP}{PL} = \frac{KQ}{QM}$	<p>A✓ construction</p> <p>A✓ method</p> <p>A✓ <math>\frac{KP}{PL}</math></p> <p>A✓ method</p> <p>A✓ <math>\frac{KQ}{QM}</math></p> <p>A✓ method</p>
	(6)



<p>9.2</p>	<p>In <math>\triangle MBC</math>: <math>\hat{BMC} = 180^\circ - (2x + 2x)</math> Sum of angles of a <math>\triangle</math></p> $= 180^\circ - 4x$ <p>But <math>\hat{BAC} = \frac{1}{2} \hat{BMC}</math> <math>\angle</math> at centre twice angle</p> $= \frac{1}{2}(180^\circ - 4x)$ $= 90 - 2x$	<p>A✓S A✓R</p> <p>A✓S/R</p> <p>(3)</p>
<p>9.3</p>	<p>In <math>\triangle ABE</math>:</p> $\hat{E}_1 + \hat{E}_2 = 180^\circ$ <p style="text-align: right;">Straight line</p> $\hat{E}_1 = 180^\circ - E_2$ $= 180^\circ - (180^\circ - 2x)$ $= 2x$ <p>In <math>\triangle ABE</math>:</p> $\hat{ABE} + \hat{BAC} + \hat{E} = 180^\circ$ <p style="text-align: right;">Sum of <math>\angle</math>s of <math>\triangle</math></p> $\hat{ABE} = 180^\circ - (\hat{BAC} + \hat{E}_1)$ $= 180^\circ - (90^\circ - 2x + 2x)$ $= 90^\circ$ <p><math>\therefore</math> AE is a diameter of circle ABE (Subtends) <math>\angle 90^\circ</math></p>	<p>A✓S/R</p> <p>A✓S</p> <p>A✓S/R</p> <p>A✓S</p> <p>A✓R</p> <p>(5)</p>
<p>[12]</p>		

**QUESTION 10**

10.1.1	Let $\widehat{Y}_1 = a$ and $\widehat{N} = b$ $\therefore \widehat{T}_3 = a - b$ (ext. $\angle$ of $\Delta =$ sum opp. $\angle$ s) $\widehat{T}_1 = \widehat{N} = b$ (tan XT; chord MT) $X\widehat{T}Y = a$ (angles opposite equal sides) $\widehat{T}_2 = X\widehat{T}Y - \widehat{T}_1$ $= a - b$ $\therefore \widehat{T}_3 = \widehat{T}_2$ $\therefore$ YT bisects $M\widehat{T}N$	A✓ S/R A✓ S A✓ R A✓ S/R  A✓ S (5)
10.1.2	In $\Delta XMT$ and $\Delta XTN$ : $\widehat{X}$ is common $\widehat{T}_1 = \widehat{N}$ tan XT; chord MT $\widehat{M}_1 = X\widehat{T}N$ remaining $\angle$ $\therefore \Delta XMT \parallel \Delta XTN$ $\angle \angle \angle$ $\therefore \frac{XM}{XT} = \frac{XT}{XN} = \frac{MT}{TN}$ similar $\Delta$ 's $\therefore \frac{XM}{XT} = \frac{XT}{XN}$	A✓ S/R A✓ S A✓ R A✓ R A✓ R  A✓ S/R (6)
10.2.1	$XM = XY - 20$ $XY = XT$ $= k - 20$	A✓ S A✓ R A✓ answer (3)
10.2.2	$\frac{XM}{XT} = \frac{XT}{XN}$  $\therefore \frac{k - 20}{k} = \frac{k}{k + 50}$ $\therefore (k - 20)(k + 50) = k^2$ $\therefore k^2 + 30k - 1000 = k^2$ $\therefore 30k - 1000 = 0$ $\therefore 30k = 1000$ $\therefore k = 33,3 \text{ mm}$	A✓ LHS A✓ RHS  A✓ Simplification  A✓ Answer (4) [18]

**TOTAL: 150**