

MATHEMATICS DEPARTMENT  
S.5 TRIGONOMETRY TEST  
TIME: 1 HOUR

**Instructions**

**Answer all questions.**

1. (a) Find the value of  $\tan A$  when  $\tan(A - 45) = \frac{1}{3}$   
  
(b) Prove that  $\tan A + \tan B = \frac{\sin(A+B)}{\cos A \cos B}$
2. (a) Prove that  $\sin 3A = 3\sin A - 4\sin^3 A$   
  
(b) Solve the equation  $3\cos 2\theta + \sin \theta = 1$  for values of  $\theta$  from  $0^\circ$  to  $360^\circ$  inclusive.
3. Find the maximum and minimum values of  $2\sin \theta - 5\cos \theta$  and state the corresponding values of  $\theta$  between  $0^\circ$  to  $360^\circ$  inclusive.
4. If  $A, B, C$  are angles of a triangle, prove that  
(a)  $\cos A + \cos B + \cos C - 1 = 4\sin \frac{A}{2} \sin \frac{B}{2} \sin \frac{C}{2}$   
  
(b)  $\tan A + \tan B + \tan C = \tan A \tan B \tan C$ .
5. (a) Prove that  $\tan 3A = \frac{3\tan A - \tan^3 A}{1 - 3\tan^2 A}$   
  
(b) Eliminate  $\theta$  from the equations  $x = \cos \theta + \sin \theta$ ,  $y = \tan \theta$

**END**