## **S5 MATHS PAPER 1/2 (ALGEBRA AND CALCULUS)**

## To be done in two weeks (23/03/2020 To 4/04/2020)

Attempt all the questions. Where possible some **hints** have been given.

- 1. Find the value of x if  $\log_x 10.24 = 2$ .
- 2. Solve the equations (i)  $\log(a^2 + 2a) = 0.9031$  (ii)  $3.2^{2x} = 8.45$
- 3. Solve the equations  $2^{x} + 4^{y} = 12$ ,  $3(2^{x}) 2(2^{2y}) = 16$ . Hence show that  $4^{x} + 4(3)^{2y} = 100$ .

Hint: Let  $a = 2^x$ ,  $b = 2^{2y}$ , form two simultaneous equations and solve them.

- 4. Solve the simultaneous equations  $2^{x+y} = 6^y$ ,  $3^x = 6(2^y)$ .
- 5. Given that  $p = \log_a(bc)$ ,  $q = \log_b(ca)$  and  $r = \log_c(ab)$ , deduce that p+q+r = pqr-2.
- 6. Express  $x^2 6x 10$  in the form  $(x+a)^2 + b$ .
- 7. Given that  $\alpha$  and  $\beta$  are the roots of the equation  $5x^2 3x + 2 = 0$ , find the equation whose roots are  $\frac{2}{\alpha 2}$  and  $\frac{2}{\beta 2}$ .
- 8. Determine the distance between the points of intersection of the curve  $5x^2 + 6xy - 8y^2 = 0$  and the line 3x - y = 7.
- 9. Find the value of x for which  $\log_2 x \log_x 4 = 1$ .
- 10. Solve the simultaneous equations.

$$2a - 3b + c = 10 \qquad 3x + y + z = 0$$
  
(i)  $a + 4b + 2c + 3 = 0$  (ii)  $x - 2y + z = 4$   
 $5a - 2b - c = 7 \qquad 2x - y - z = 5$ 

Hint: In (i) and (ii), by eliminating *one of the letters*; taking any two equations at a time, we can solve the equations.

11. Express  $\frac{1+\sqrt{3}}{(\sqrt{3}-1)^3}$  in the form  $a+b\sqrt{c}$ .

- 12. Find the maximum value of  $1 5x 2x^2$  and the value of x for which it occurs.
- 13. Solve the equations (i)  $2\sqrt{x} \sqrt{x+5} = 1$  (ii)  $\sqrt{p+6} \sqrt{p+3} = \sqrt{2p+5}$ .
- 14. If  $y = a + bx^n$  is satisfied by the values in the table below,

x	1	2	4
у	7	10	15

Show that  $n = \log_2 \frac{5}{3}$  and deduce the values of *a* and *b*.(Hint: Form 3 equations and solve them simultaneously)

15. Solve the equations:

(i) 
$$\log(x-1) + 2\log y = 2\log 3$$
,  $\log x + \log y = \log 6$ 

(ii) 
$$\log_2 x^2 + \log_2 y^3 = 1$$
,  $\log_2 x - \log_2 y^2 = 4$ 

Hint: Apply laws of logs

- 16. Solve the equations
  - (i)  $\log_{2x} 4 = \log_4 x$  (ii)  $(\log_3 x) \cdot (\log_{3x} 3) = \frac{3}{4}$

(iii)  $2\sqrt{x} + \sqrt{2x+1} = 7$  (iv)  $t^2 + 2t = 34 + 35/(t^2 + 2t)$ 

- 17. The points O, R and S have coordinates (0, 0), (4, 3) and (a, b) respectively. Given that OR and RS are perpendicular,
  - (i) show that 4a + 3b = 25, (ii) find the value of a if b = 4.
- 18. Line  $L_1$  is defined by the equation 2x + y = 1.  $L_2$  is a line through point (2, -1) and is perpendicular to line  $L_1$ . Calculate the perpendicular distance of the point (0, -4) from  $L_2$ .
- 19. A triangle ABC has sides with equations 3x y = 3, x y 1 = 0 and 3x 5y = -9 respectively. Find the area of the triangle ABC.
- 20. The points A and B have coordinates (2, 4) and (1, -3) respectively. Determine the coordinates of the point T which divides AB internally in the ratio 2:1.
- 21. Calculate the acute angle between the straight lines 3x-y=5 and x+4y=11. (Use two methods)