S475/1
SUB - MATHEMATICS
Paper 1
June/July, 2016
$2 / 3$ hours

# MOCK EXAMINATIONS 2016 

Uganda Advanced Certificate of Education SUB - MATHEMATICS

Paper 1
2 hours 40 minutes

## INSTRUCTIONS

- Answer all the eight questions in section $A$ and only four questions in section $B$.
- Any additional question(s) answered will not be marked
- All working must be shown clearly
- Begin each answer on a fresh page
- Graph paper is provided
- Avoid mixing the two sections $A$ and $B$
- Non - programmable scientific calculators may be used.


## SECTION A (40 MARKS)

## Answer all the questions in this section

1. Given that $a=\log _{x} x y^{2}$ and $b=\log _{x} x^{3} y^{-2}$, find the value of $a+b$
2. The table below shows the heights of trees in meters in a certain forest. Calculate the standard deviation

| Height in meters | $15-$ | $20-$ | $25-$ | $30-$ | $35-$ | $40-45$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of trees | 2 | 14 | 29 | 43 | 33 | 9 |

3. The table below shows the price of items and their corresponding weights in the years 2000 and 2004.

| ITEM | PRICE (Ushs) | PRICE | Weight |
| :--- | :--- | :--- | :--- |
|  | 2000 | 2004 |  |
| Food | 55,000 | 60,000 | 2 |
| Housing | 48,000 | 52,000 | 1 |
| Transport | 16,000 | 20,000 |  |

Using 2000 as the base year, calculate the weighted price index for the items in 2004.
4. A box contains 4 black pens (B) and 5 red pens (R). Two pens are picked at random, one after the other without replacement. Find the probability that both pens are of the same.
5. Events A and B are independent.
(a) Show that events A and $B^{1}$ are also independent.
(b) If $P(A)=\frac{1}{5}$ and $P\left(B^{1}\right)=\frac{2}{3}$, find $P\left(A \cup B^{\prime}\right)$.
6. The roots of the quadratic equation $x^{2}-p x+q=0$ are $\propto$ and $\beta$. Form an equation in terms of $P$ and $q$ whose roots are $\frac{1}{2 \alpha} a b d \frac{1}{2 \beta}$.
7. Solve the equation $2^{x} 2^{1-x}-3=0$.
8. Given that $\frac{3-2 \sqrt{3}}{3+2 \sqrt{3}}-\frac{3+2 \sqrt{3}}{3-2 \sqrt{3}}=a+b \sqrt{3}$, find rational values of $a$ and $b$.

## SECTION B

9. Eight candidates seeking admission to senior one sat for English and math tests. The scores were as shown in the table below.

| English (x) | 55 | 54 | 35 | 62 | 87 | 56 | 71 | 50 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Maths (y) | 57 | 60 | 47 | 65 | 83 | 53 | 74 | 63 |

(a) (i) Draw a scatter diagram for the data
(ii) Draw a line of best fit on your scatter diagram.
(iii) Use the line of best fit to find the value of $y$ when $x=70$.
(08 marks)
(b) Calculate Spearman's rank correlation coefficient. Comment on your result (07 marks)
10. The table below shows the number of boxes of pens sold by a certain wholesale shop from the year 2009 to 2012.

| Year | Quarter |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $1^{\text {st }}$ | $2^{\text {nd }}$ | $3^{\text {rd }}$ | $4^{\text {th }}$ |
| 2009 | 192 | 280 | 320 | 260 |
| 2010 | 300 | 360 | 380 | 270 |
| 2011 | 342 | 420 | 430 | 320 |
| 2012 | 424 | 480 | 510 | 412 |

(a) Calculate the four - point moving averages for the data ( 06 marks)
(b) (i) On the same axes, plot the original data and the four - point moving averages.
(05 marks)
(ii) Comment on the trend of the number of boxes of pens sold over the four - year period.
(iii) Use your graph to estimate the number of boxes to be sold in the first quarter of 2013.
11. Differentiate the following with respect to $X$.
(a) $Y=\left(3 x^{2}-5 x\right)^{-2 / 3}$
(b) $Y=\left(1+X^{2}\right)^{2}\left(1-x^{2}\right)$
(c) $Y=3 x^{4}-8 x^{3}-6 x^{2}+24 x+3$
(d) $Y=\frac{x^{2}+}{(x+2)^{2}}$
12. (a) Simply $\frac{x^{2}\left(x^{2}+1\right)-\frac{1}{2}-\left(x^{2}+1\right)^{\frac{1}{2}}}{x^{2}}$
(b) Without using tables or calculators, find the values of
(i) $\frac{12^{3 / 2} \times 16^{1 / 8}}{27^{\frac{1}{6} \times 18^{\frac{1}{2}}}}$
(ii) $\log 75+2 \log 2-\log 3$
(c) Show that $2 x^{2}+x^{2}-13 x+6$ is divided by $x-2$, and hence find the other factors of the expression.

